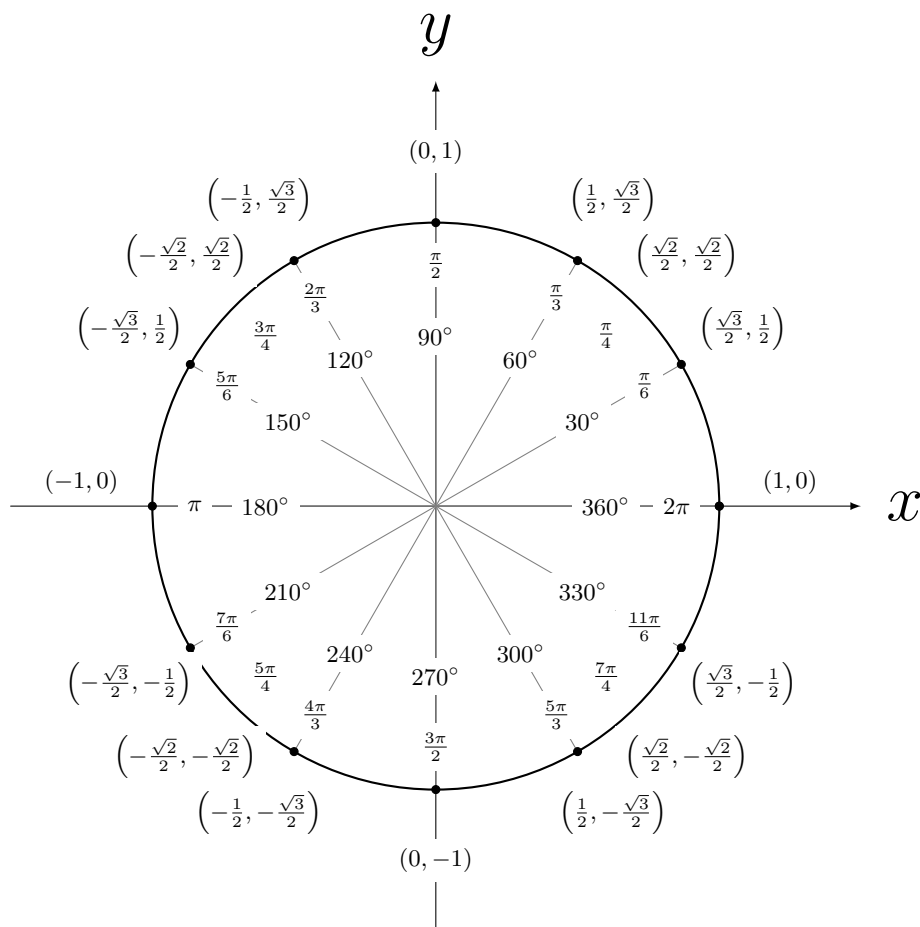


# Trigonometry

## The Unit Circle:



- This is a circle of radius one. The prefix uni- means one. Thus, the unit circle has a radius equal to one.
- The equation for the unit circle is  $x^2 + y^2 = 1$ .
- The circumference of any circle is  $2\pi r$ , thus the circumference of the unit circle is  $2\pi$ .
- $\frac{1}{4}$  of the distance around the unit circle is  $\frac{\pi}{2}$
- $\frac{1}{2}$  of the distance around the unit circle is  $\pi$
- $\frac{3}{4}$  of the distance around the unit circle is  $\frac{3\pi}{2}$
- the full distance around the unit circle is  $2\pi$

**NOTE:** Any point on the unit circle has a coordinate  $(x, y)$ . If we draw a right triangle from the origin,  $(0, 0)$ , to the point on the unit circle,  $(x, y)$ , to the point on the  $x$ -axis,  $(x, 0)$ , we can use the following formulas for sine, cosine, and tangent to show that for any point on the unit circle that:

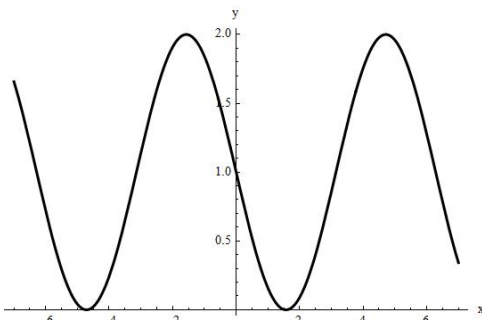
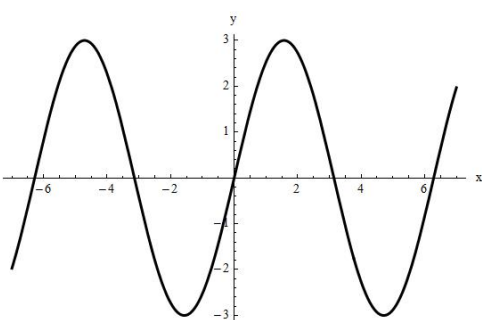
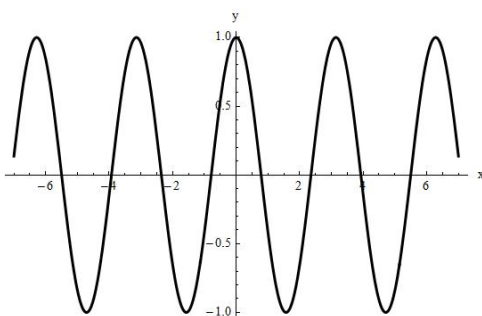
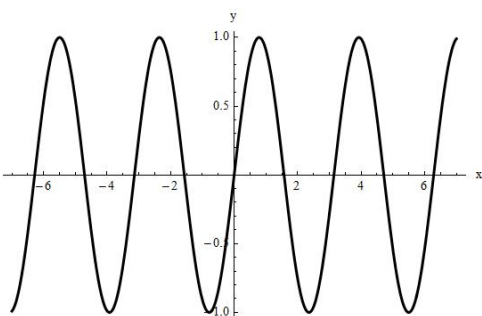
$$\cos \theta = \frac{x}{r} = \frac{x}{1} = x$$

$$\sin \theta = \frac{y}{r} = \frac{y}{1} = y$$

$$\tan \theta = \frac{y}{x}$$

Match four of the following functions to the graphs below; then, graph the remaining two functions.

- a.  $f(x) = 1 + \sin x$     b.  $g(x) = 1 - \sin x$     c.  $h(x) = 3 \sin x$   
 d.  $r(x) = \cos 2x$         e.  $s(x) = 3 \sin(x)$     f.  $m(x) = \sin 2x$



# Radians and Degrees

Conversions:

$$\begin{aligned}1 \text{ radian (rad)} &= \left(\frac{180}{\pi}\right) \text{ degrees } (^\circ) \\ \pi \text{ radians} &= 180 \text{ degrees} \\ 1 \text{ degree} &= \left(\frac{\pi}{180}\right) \text{ radians}\end{aligned}$$

1. Find the radian measure of the angle when given the degree measure:

$$\begin{aligned}a. \quad 36^\circ & \quad b. \quad 200^\circ & \quad c. \quad 45^\circ \\ d. \quad -72^\circ & \quad e. \quad 60^\circ & \quad f. \quad 115^\circ \\ g. \quad -135^\circ & \quad h. \quad 150^\circ & \quad i. \quad -420^\circ\end{aligned}$$

2. Find the degree measure of the angle with the following radian measure:

$$\begin{aligned}a. \quad \frac{3\pi}{4} \text{ rad} & \quad b. \quad -\frac{7\pi}{2} \text{ rad} & \quad c. \quad \frac{5\pi}{6} \text{ rad} \\ d. \quad -\frac{\pi}{12} \text{ rad} & \quad e. \quad -1.5 \text{ rad} & \quad f. \quad \frac{2\pi}{9} \text{ rad} \\ g. \quad \frac{\pi}{5} \text{ rad} & \quad h. \quad \frac{\pi}{18} \text{ rad} & \quad i. \quad \frac{5\pi}{3} \text{ rad}\end{aligned}$$

# Trigonometric Identities

Simplify the following trigonometric expressions:

- $(\sin \theta)^2 + (\cos \theta)^2 - 1$
- $(\sin \theta + \cos \theta)^2 + 2 \cos \theta$
- $(\sin \theta)(\cos \theta) + (\sin \theta)^3 - 2$
- $2(\cos \theta)^2 + 2(\sin \theta)^2 + 1$